

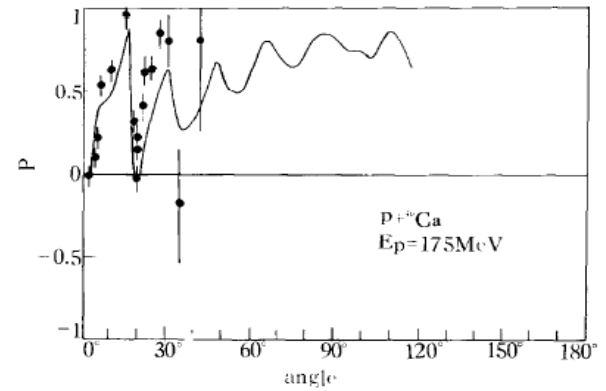
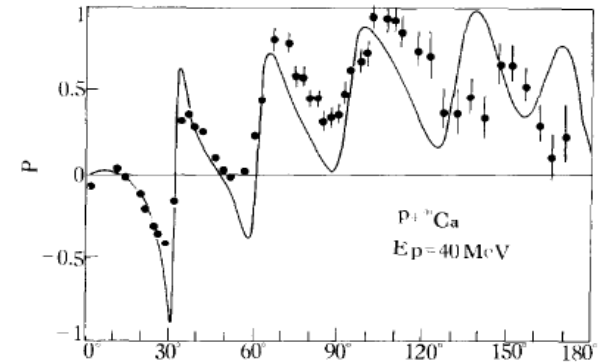
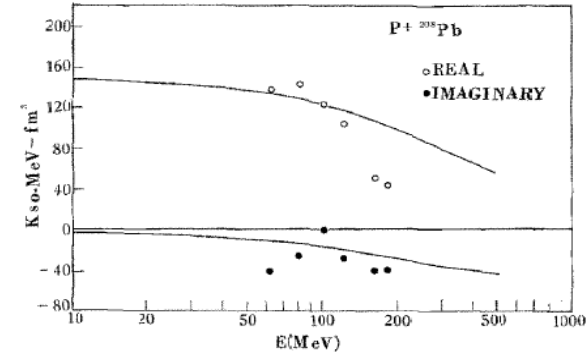
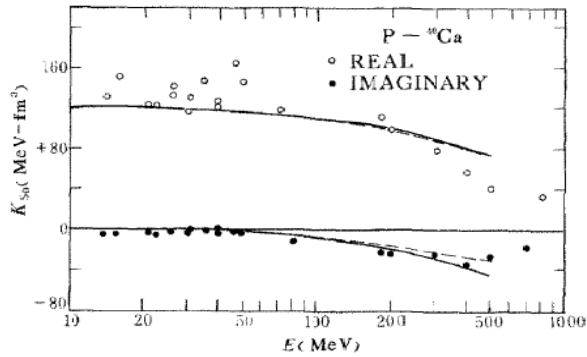
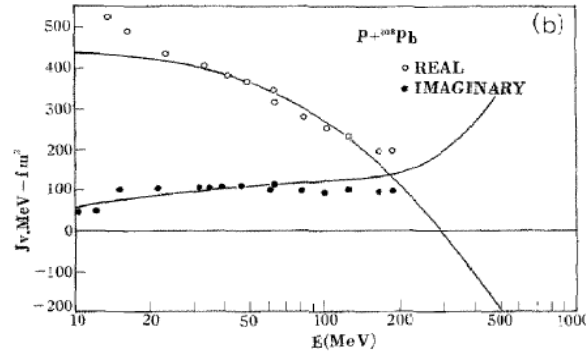
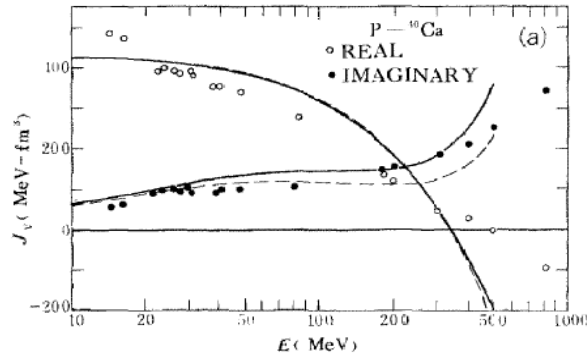


Microscopic Optical Potential in Relativistic Approach

Zhongyu Ma



Microscopic Optical Model Potentials



Volume integrals

Analyzing power



Introduction

- Current interests of OMP:

The dependence of N-A, A-A scattering potentials (OMP) on

$$\rho, \quad k \text{ (or } E), \quad \beta = (\rho_n - \rho_p) / \rho$$

Extension to high densities, energies and isospin dependence

- Two levels of approaches in studying the microscopic OMP

- Phenomenological nuclear effective int

Skyrme force, M3Y(DDM3Y),

RMF based on isoscalar meson exchanges

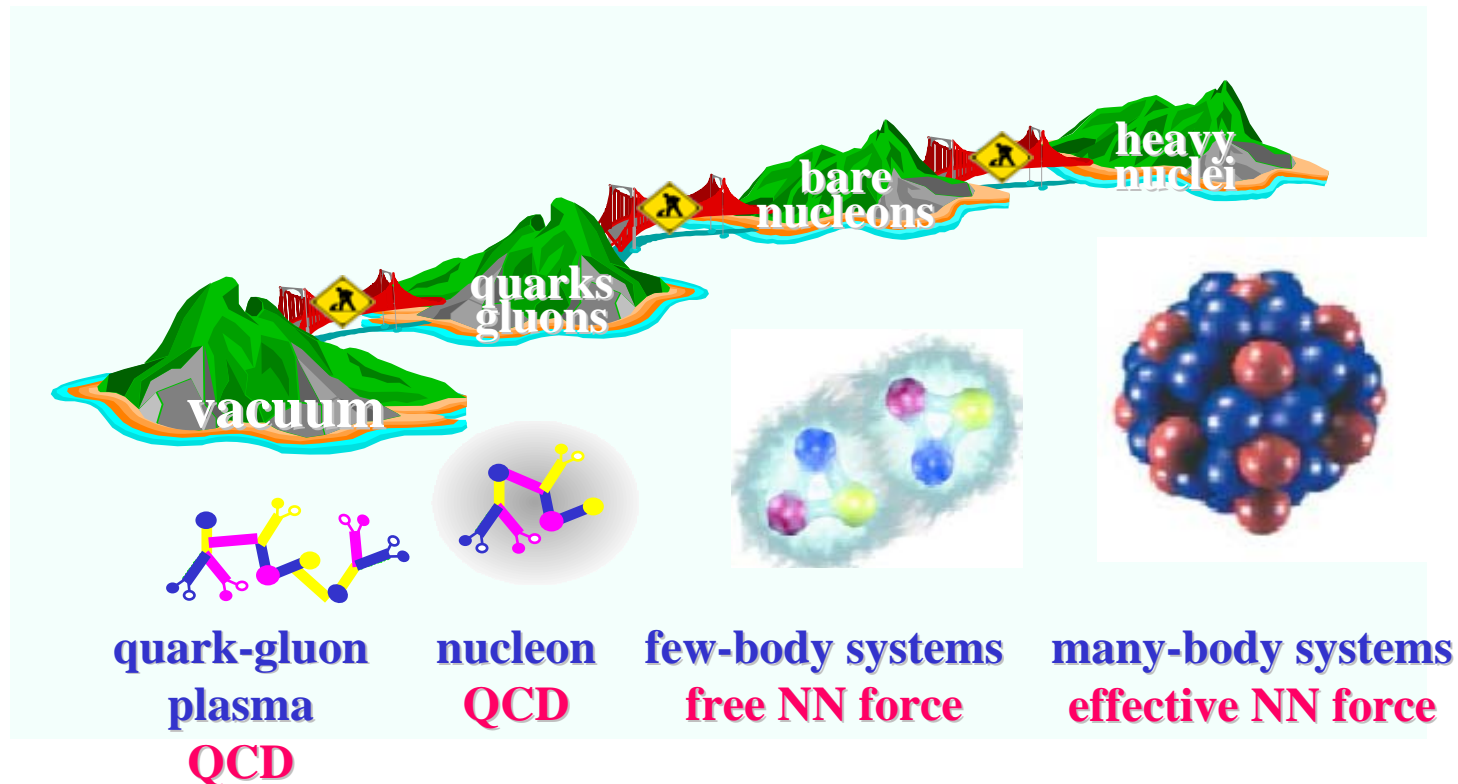
- Microscopic approaches from bare NN interactions

BHF

DBHF

Open Problems in Nuclear Structure Theory

From simplicity to Complexity





The Dirac–Brueckner–Hartree–Fock approach: from infinite matter to effective Lagrangians for finite systems

Nguyen Van Giai¹, Brett V Carlson², Zhongyu Ma³ and Hermann Wolter⁴

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Microscopic calculations of OMP

- Non relativistic approaches

BHF with bare NN int. can not apply to high densities

 saturations are not well reproduced

J.-P.Jeukenne, A.Lejeune,C.Mahaux, PRC16(77)80

(JLM model)

BHF with bare NN + 3body int.

Real + Imaginary OMP at asymmetric NM

Li, Lombardo, Schulze, Zuo PRC77(08)034316

Li, Li, Zhao EG, Zhou SG, Zuo W, PRC80(09)064607

Spin-orbit interactions are put by hand

- Relativistic approaches

NN + DBHF

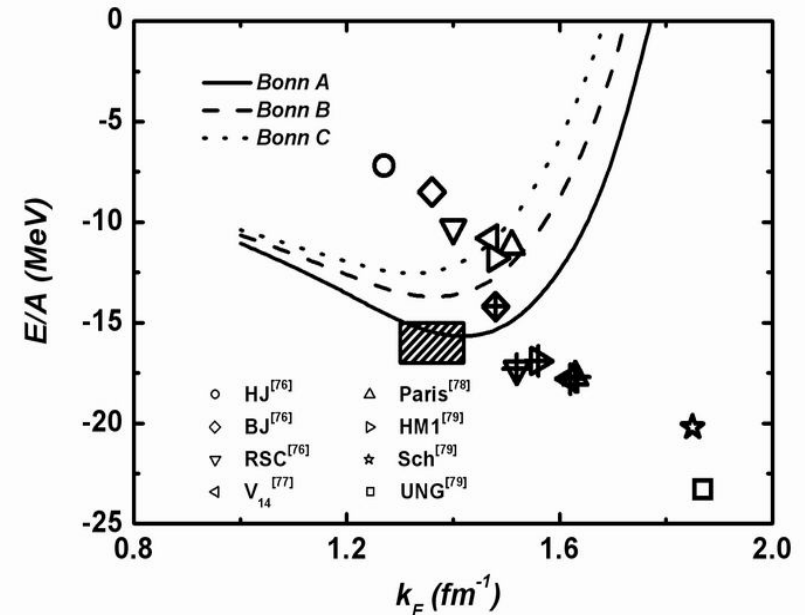
Success in description of
NM saturation properties

- OMP of nucleon in the nuclear matter is equivalent to the self energy of nucleon

Finite nuclei: LDA

$\Sigma(k, k_F, \beta)$ dep. \rightarrow $\Sigma(E, r)$ dep.

spin-orbit pot's are obtained naturally





Self-consistency DBHF

- Three dimension reduction -- the relativistic Thompson equation

$$T(\mathbf{p}, \mathbf{q}, x)|_{\text{c.m.}} = V(\mathbf{p}, \mathbf{q}) + \int \frac{d^3\mathbf{k}}{(2\pi)^3} V(\mathbf{p}, \mathbf{k}) \frac{m_F^{*2}}{E^{*2}(\mathbf{k})} \frac{Q(\mathbf{k}, x)}{2E^*(\mathbf{q}) - 2E^*(\mathbf{k}) + i\epsilon} T(\mathbf{k}, \mathbf{q}, x)$$

the time-like component of the momentum transfer in V and T is set equal to zero

- Self-consistent calculations is important

$T \xrightarrow{?} \Sigma \rightarrow \text{Dirac eq.} \rightarrow \text{s.p. wf}$

T matrix --- do not keep the track of rel. structure

Extract the nucleon self-energy with single particle energy

$$\varepsilon_i(k) = \sqrt{k^2 + [M + U_s^i(k)]^2} - U_0^i(k) \quad \text{weak momentum dep.}$$

$$\Sigma(k) \approx \Sigma(|k| = k_F) \longrightarrow \varepsilon_i(k) = \sqrt{k^2 + [M + U_s^i]^2} - U_0^i$$



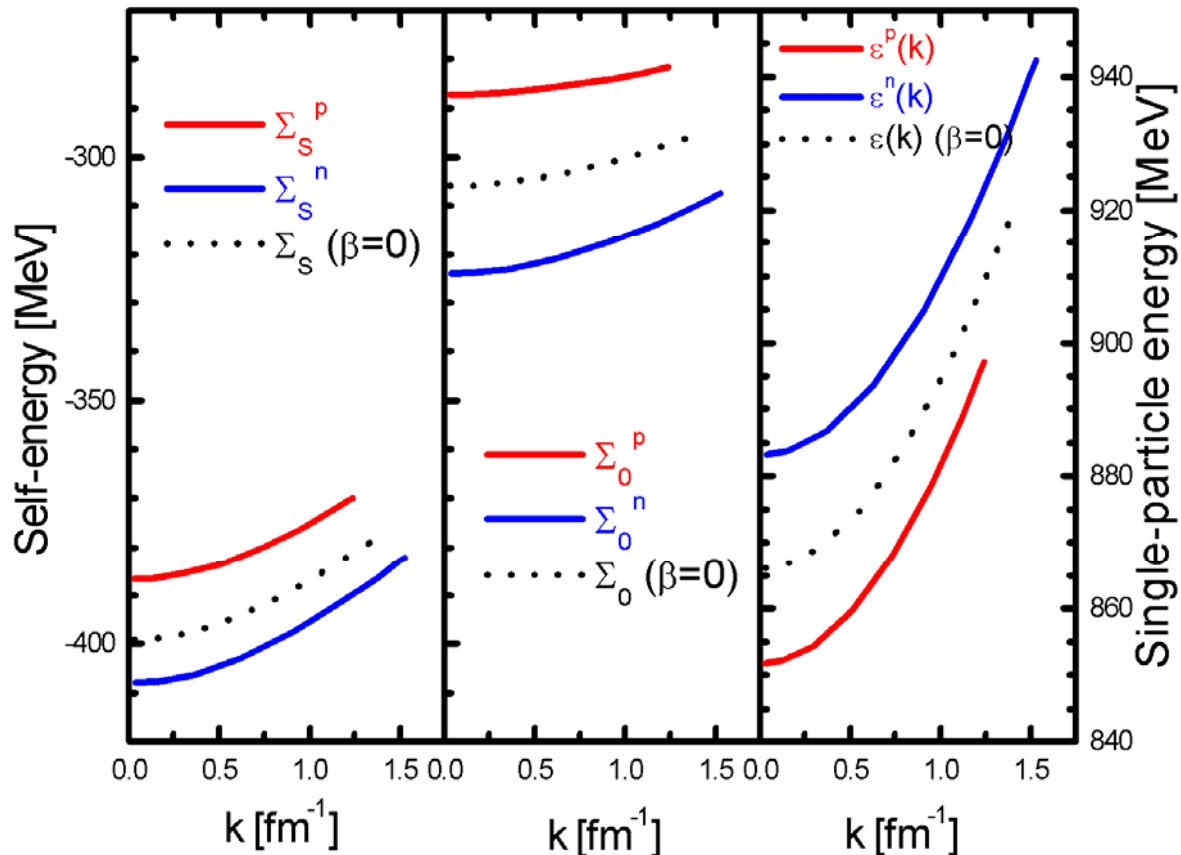
Difficulties in asymmetric NM

Us, Uo have different behavior of E dep. in asymmetric NM

$$\varepsilon_i(k) = \sqrt{k^2 + [M + U_s^i]^2} - U_0^i$$

This simple assumption
fails in asymmetric nuclear
matter

Wrong behavior of
Isospin dependence
of self-energies
In asymmetric NM





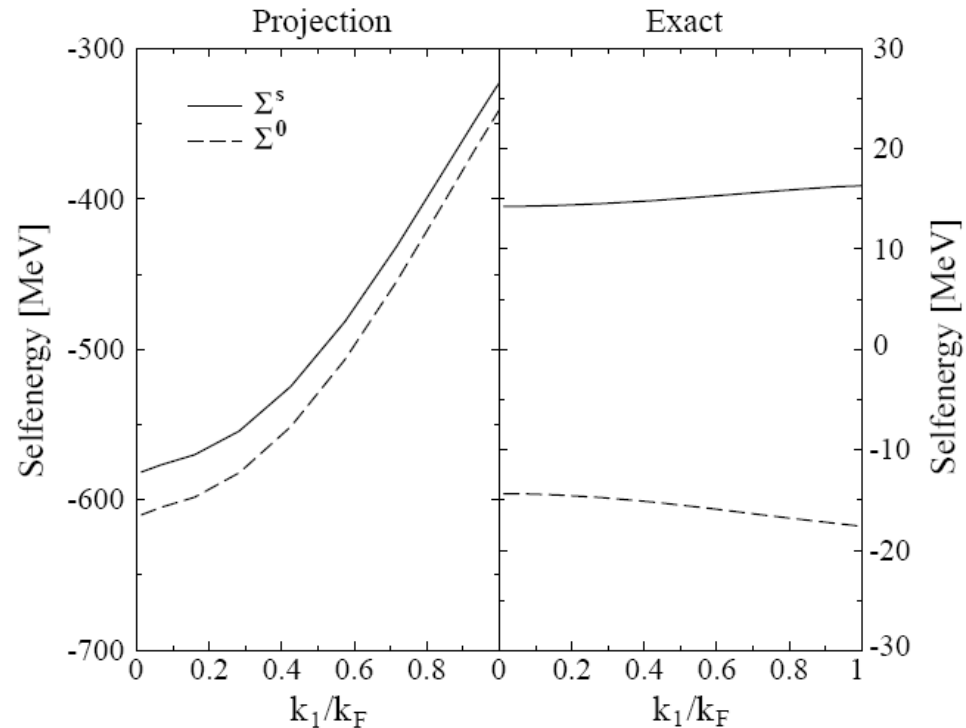
Isospin dependence of OMP

- Projection methods

$$T \rightarrow \{1, \gamma^\mu, \sigma^{\mu\nu}, \gamma^5 \gamma^\mu, \gamma^5\}$$

Due to the restriction to positive energy states

Give a unphysical strong momentum dependence in the self-energy



originate mainly from the one-pion exchange contribution to the self-energy



Decomposition of T

- Decomposition of DBHF T matrix

$$T = V + \Delta T$$

V : OBEP $\sigma \omega \eta \delta \rho \pi$

ΔT a projection method

$$\Delta T = \left[g_{s,s} 11 + g_{v,s} \gamma^\mu \gamma_\mu \right] + \left[g_{s,v} 11 + g_{v,v} \gamma^\mu \gamma_\mu \right] \tau \cdot \tau$$

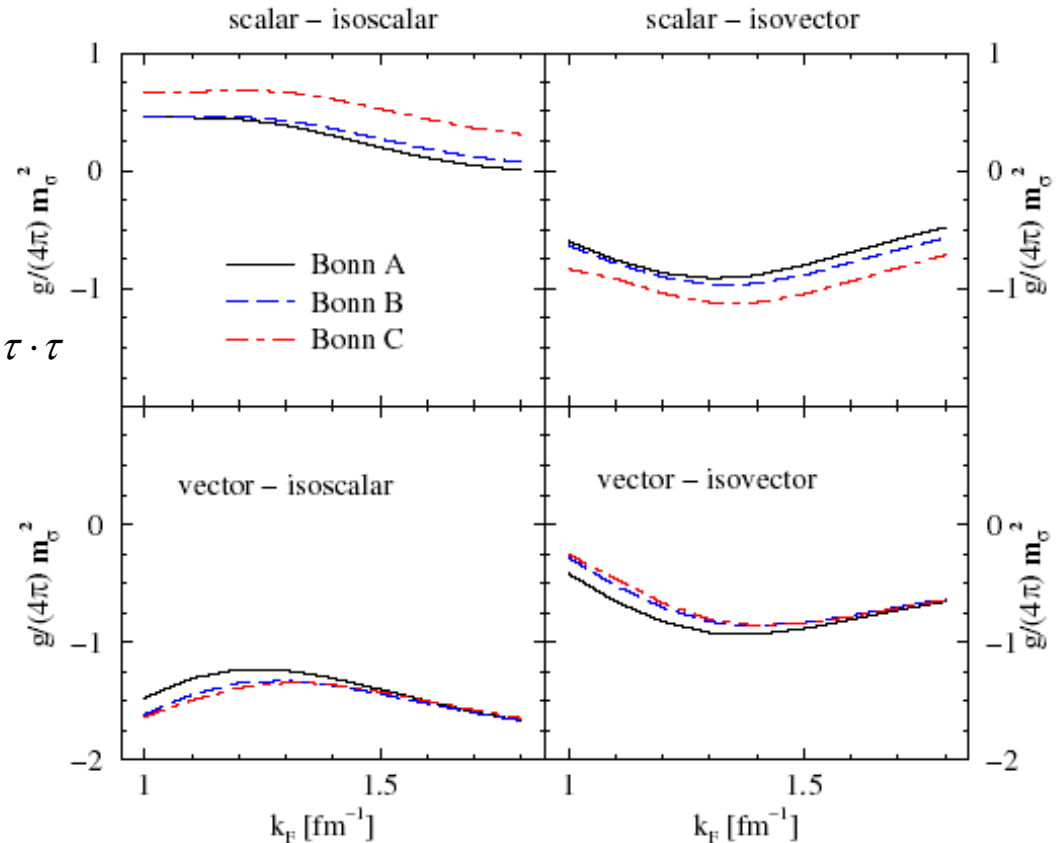
$$(1, \gamma_\mu) \quad (1, \tau)$$

Short range

$m \rightarrow \infty \quad (g/m)^2 \rightarrow \text{finite}$

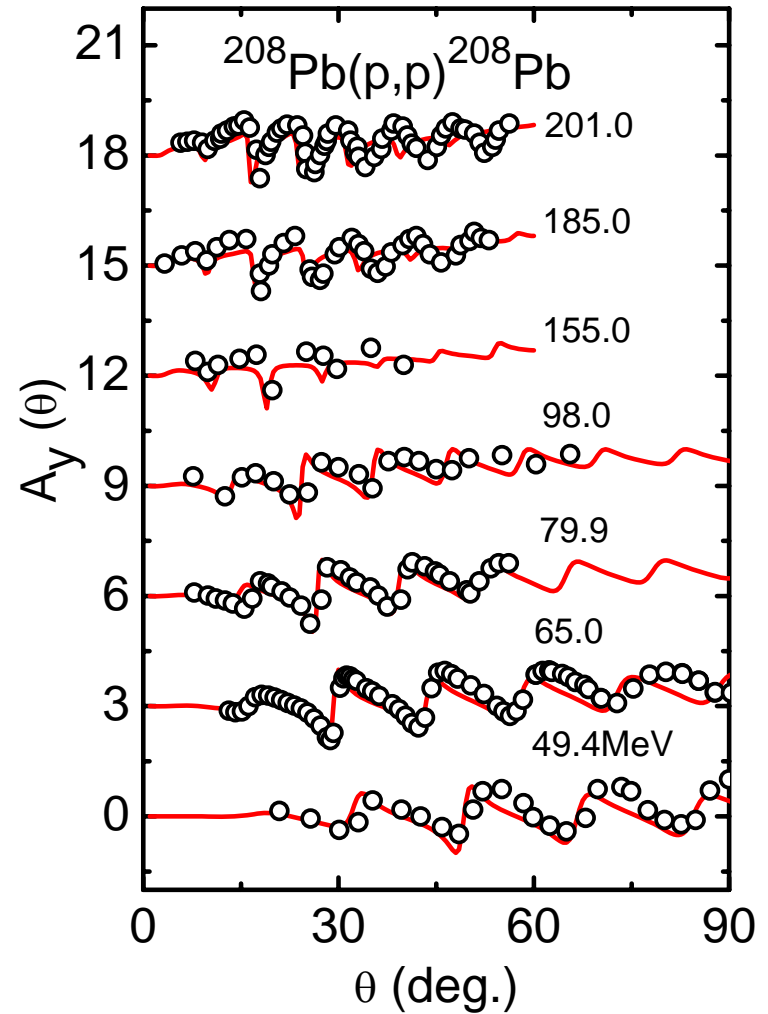
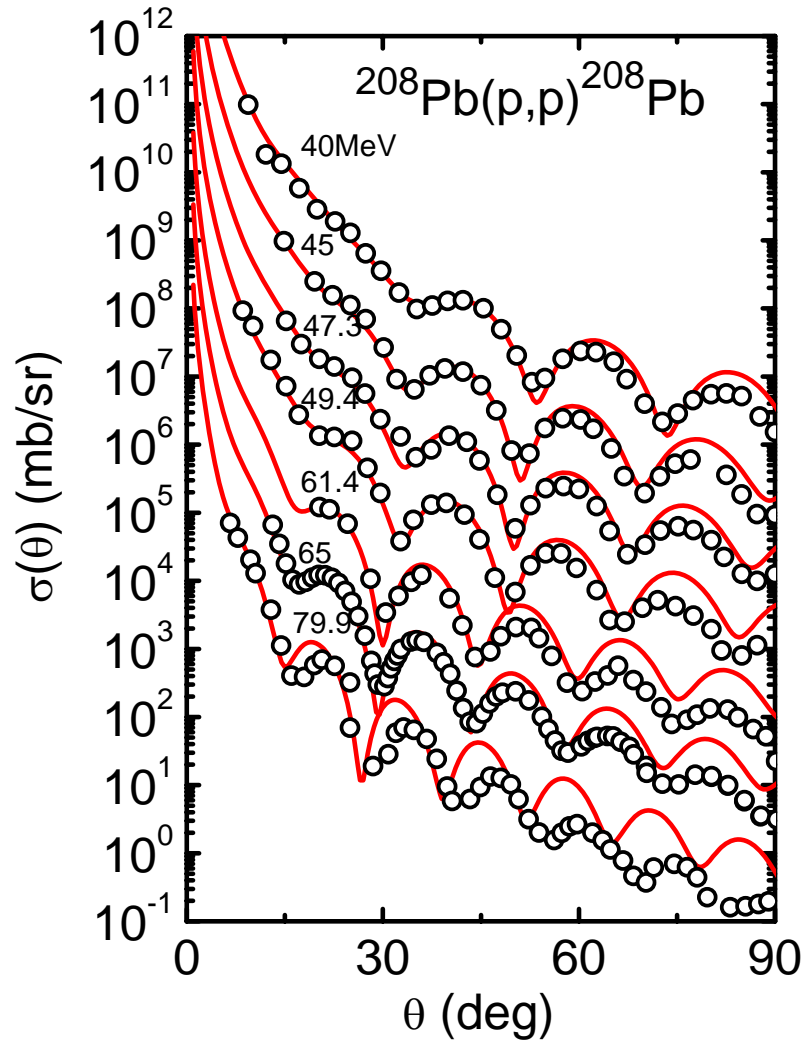
E. Shiller, H. Muether,

E Phys. J. A11(2001)15





$^{208}\text{Pb} (p, p) ^{208}\text{Pb}$



J. Rong, Z. Y. Ma, PRC 06



Optical potential of Nucleus-Nucleus Scatterings

$$U_s^p, U_0^p$$

$$U_s^n, U_0^n$$



$$V_{eff}^{p(n)}(r)$$

folding



$$V_{DFM}(\mathbf{R}) = \int \rho_1(\mathbf{r}_1) \rho_2(\mathbf{r}_2) V_{eff}(s, \rho, \varepsilon) d\mathbf{r}_1 d\mathbf{r}_2$$

Real & Imaginary

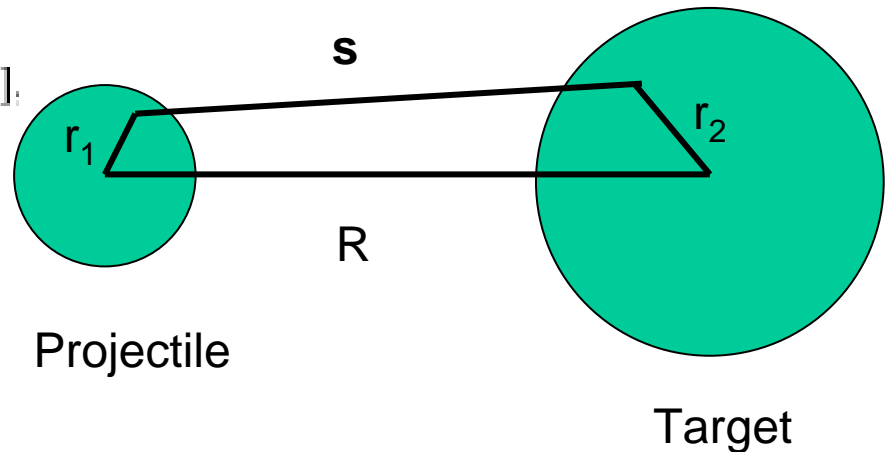
Schroedinger eq. pot. U

Real & Imaginary

$$U_{eff} = \frac{M}{E} U_s + U_0 + \frac{1}{2E} [(U_s)^2 - (U_0 + V_C)^2]$$

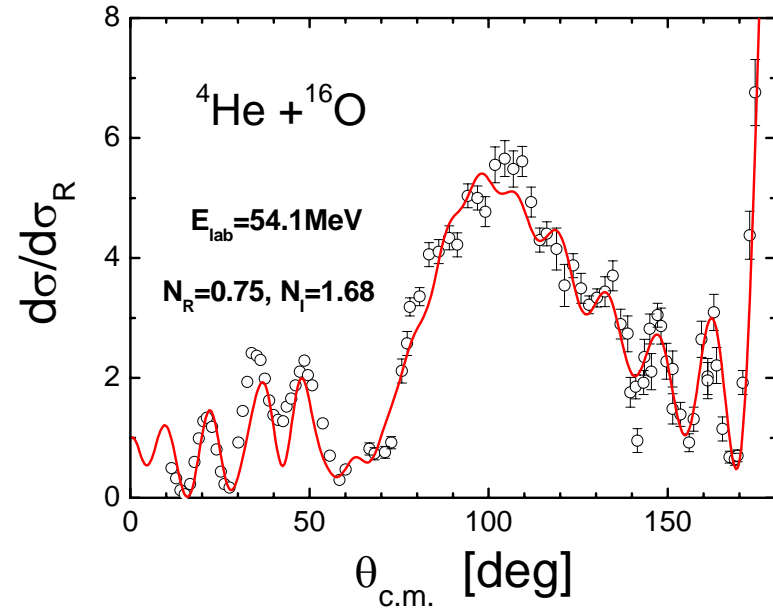
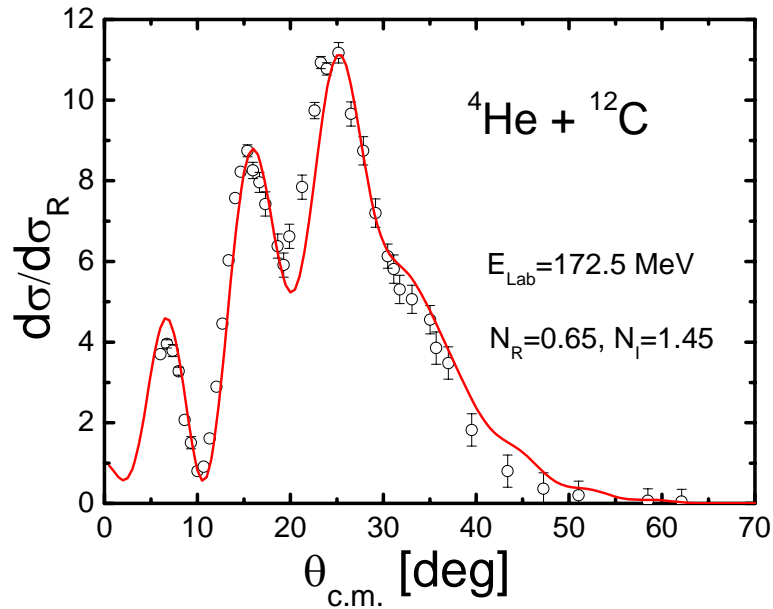
The NN effective interaction in the nuclear medium

$$V_{eff} = U_{eff} / \rho$$





α -nucleus scatterings

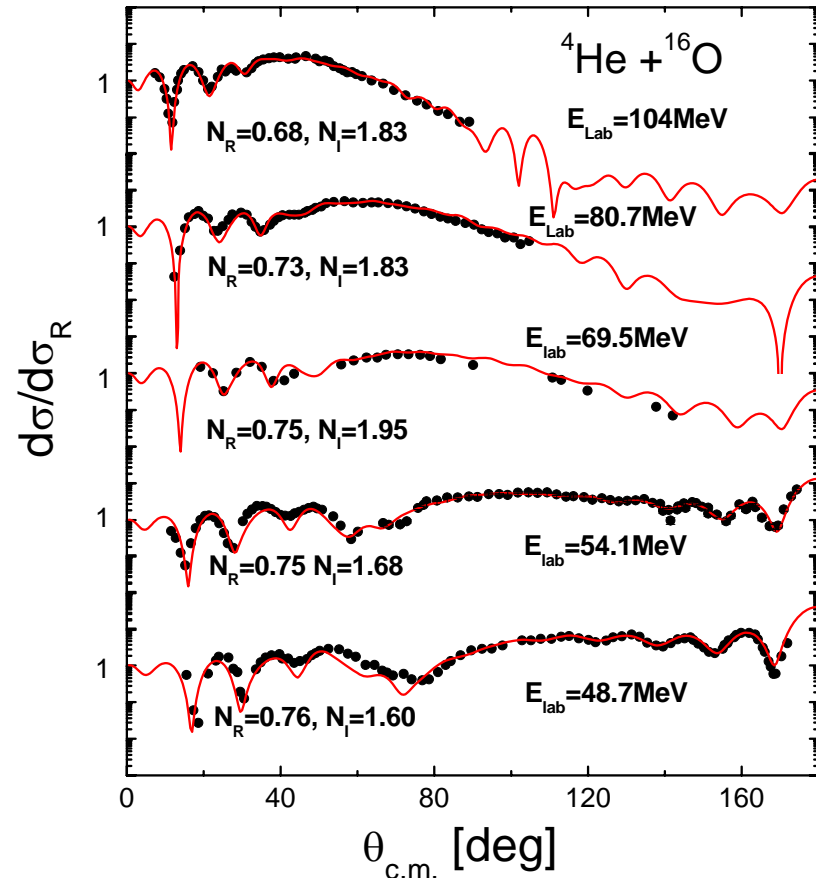
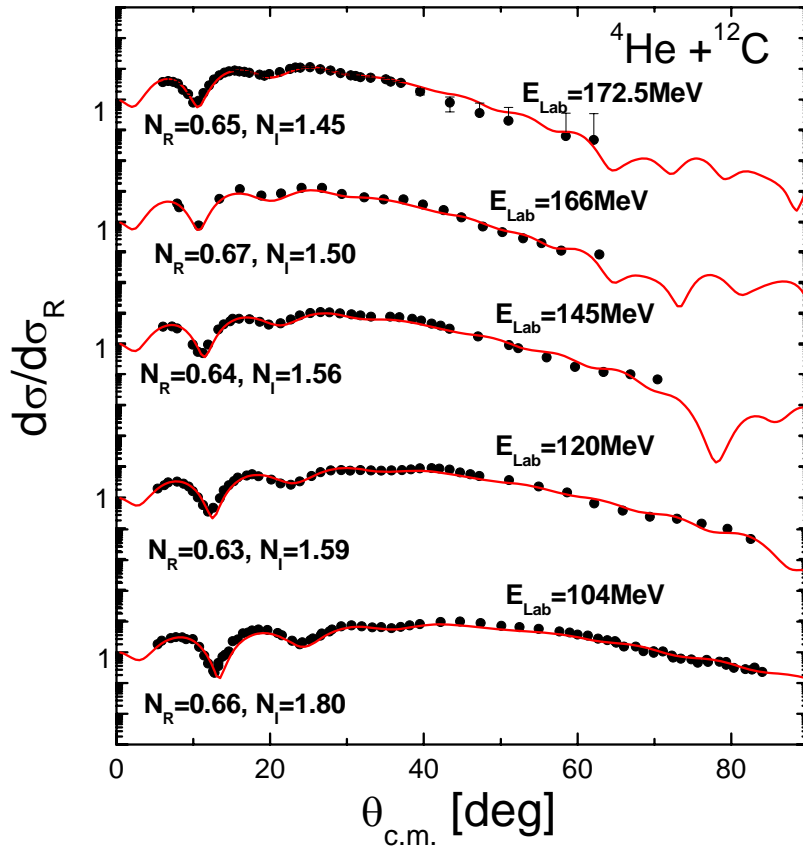


the cross sections calculated with the nucleon effective interaction based on the DBHF reproduce the experimental data quite well.

W Zou, Y Tian, and ZY Ma **78**, 064613 (2008)



α -nucleus scatterings



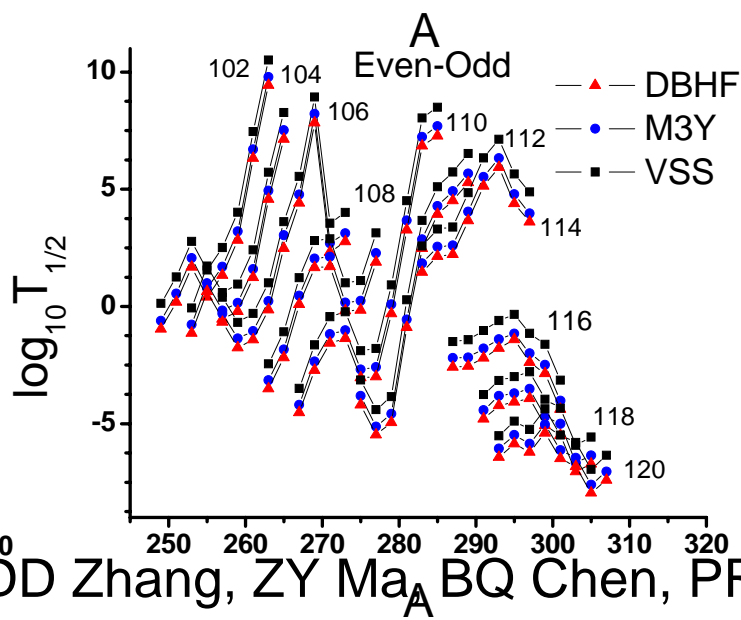
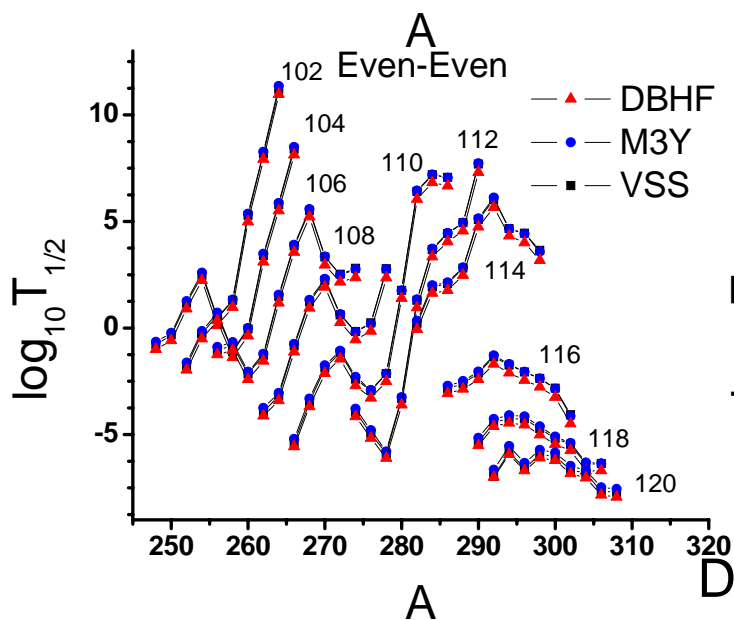
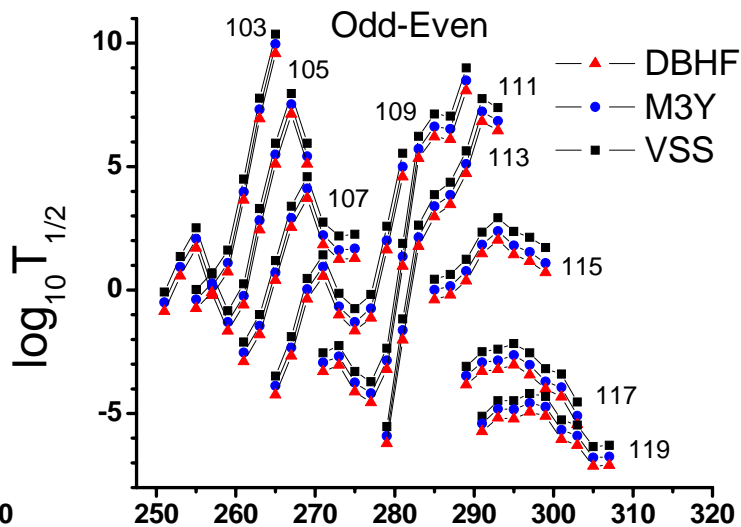
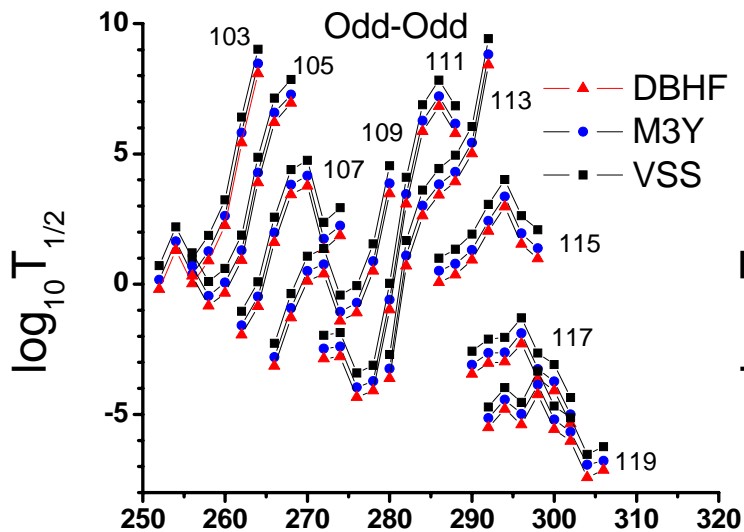
the renormalization factors are weak dependence on the energy

$$N_R \approx 0.63-0.67, N_I \approx 1.5-1.8$$

$$N_R \approx 0.7-0.75, N_I \approx 1.7-1.8$$



α -decay half-lives of superheavy elements





DBHF in asymmetric NM

- Subtracted G-matrix representation

the influence of the pion is dominantly given by the **single-pion exchange**,

reasonable to treat the bare interaction of the π and η separately to the rest.

After subtraction of the bare interaction of the η - and π -meson the remainder is the subtracted G -matrix,

$$T_{\text{Sub}} = T - V_{\pi\eta}$$

E. N. E. van Dalen, C. Fuchs, and Amand Faessler, Nucl. Phys. **A744**, 227 (2004); Eur. Phys. J. A **31**, 29 (2007).



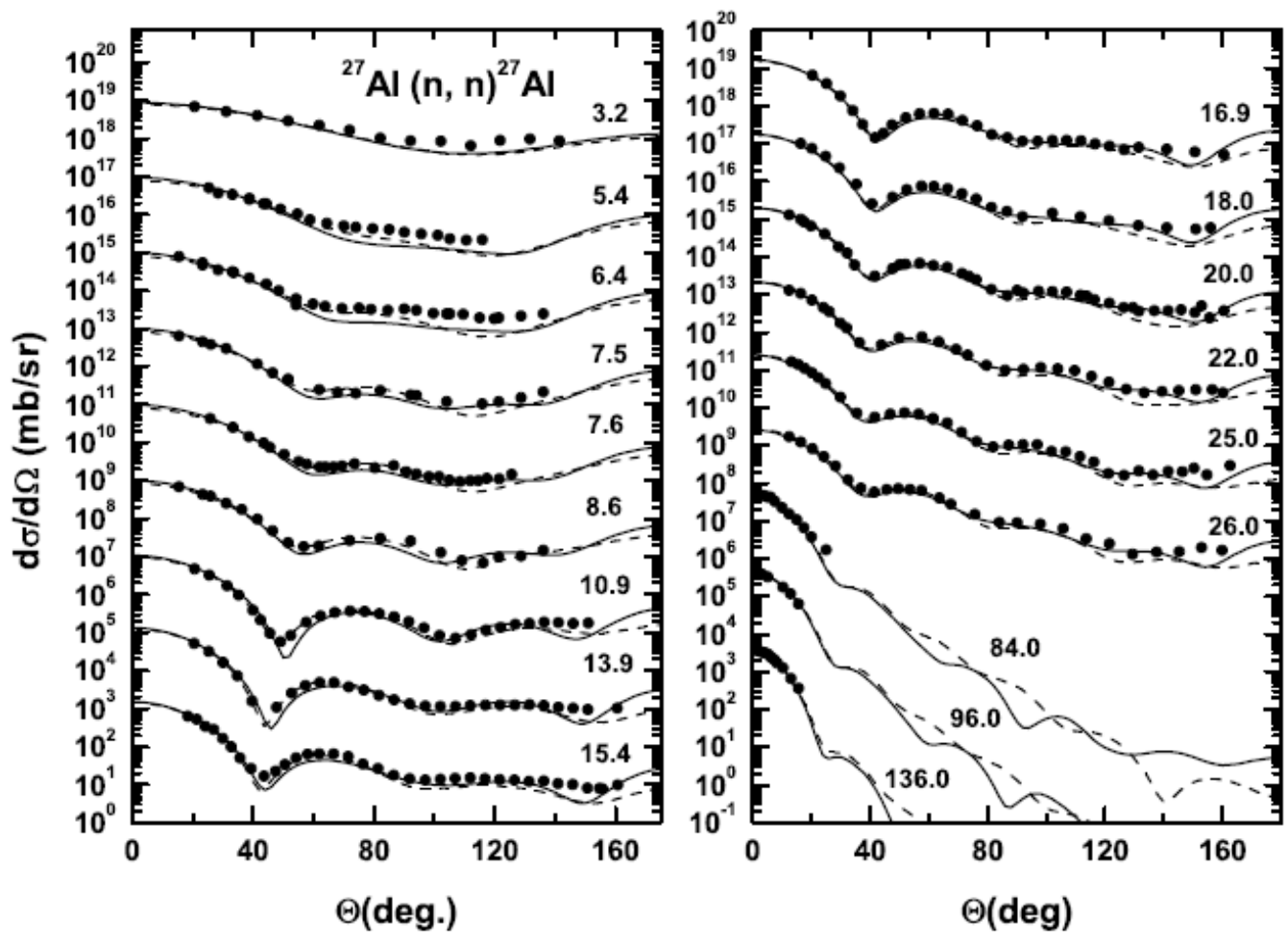
Systematic Study of RMOP

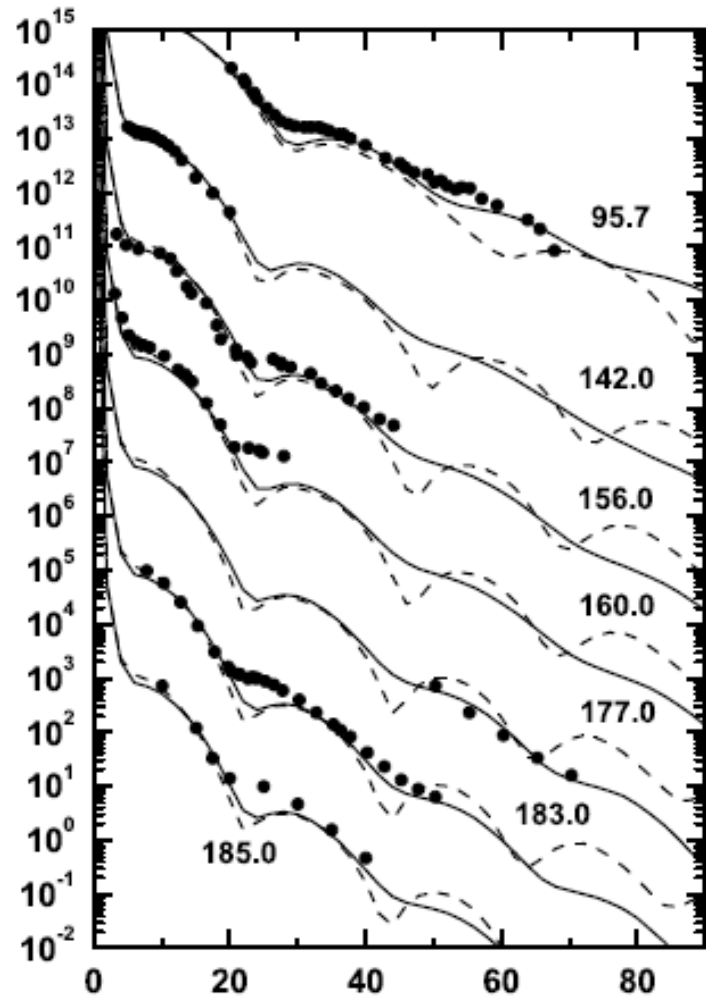
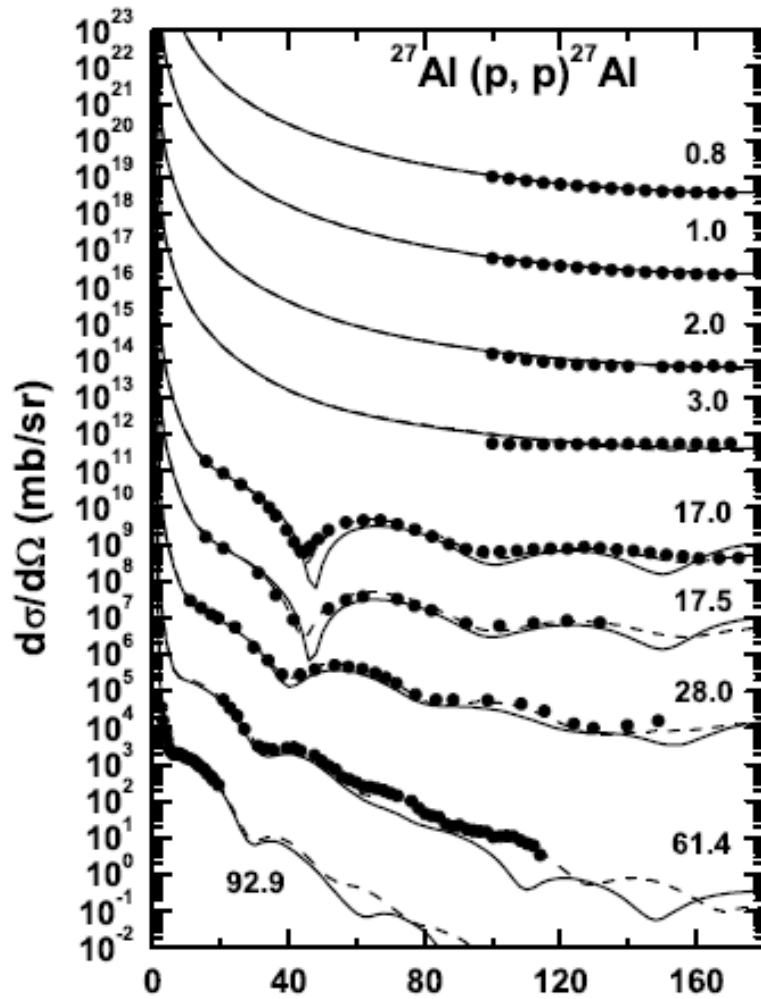
Energy region: 0.1 — 250MeV

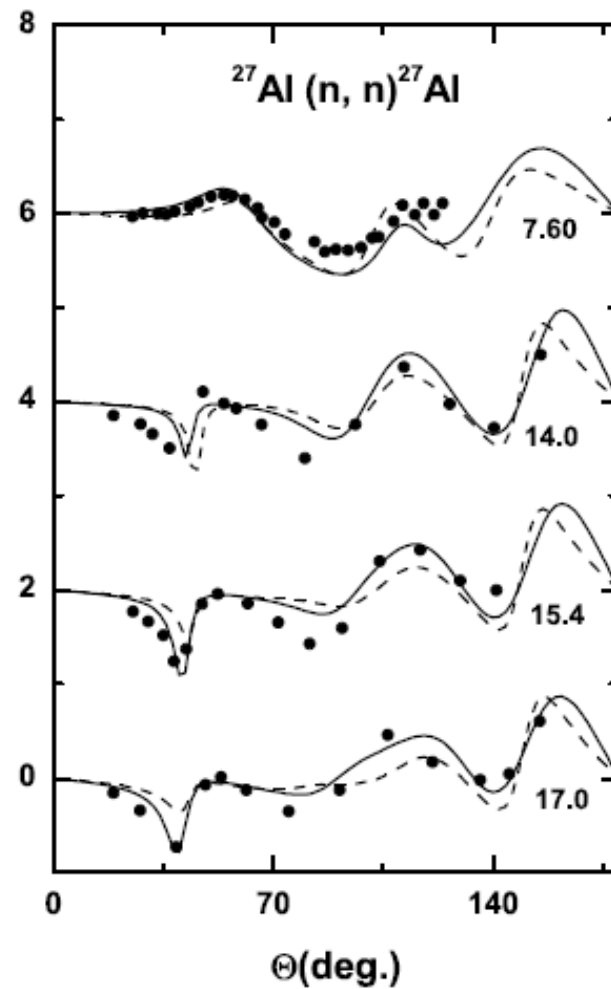
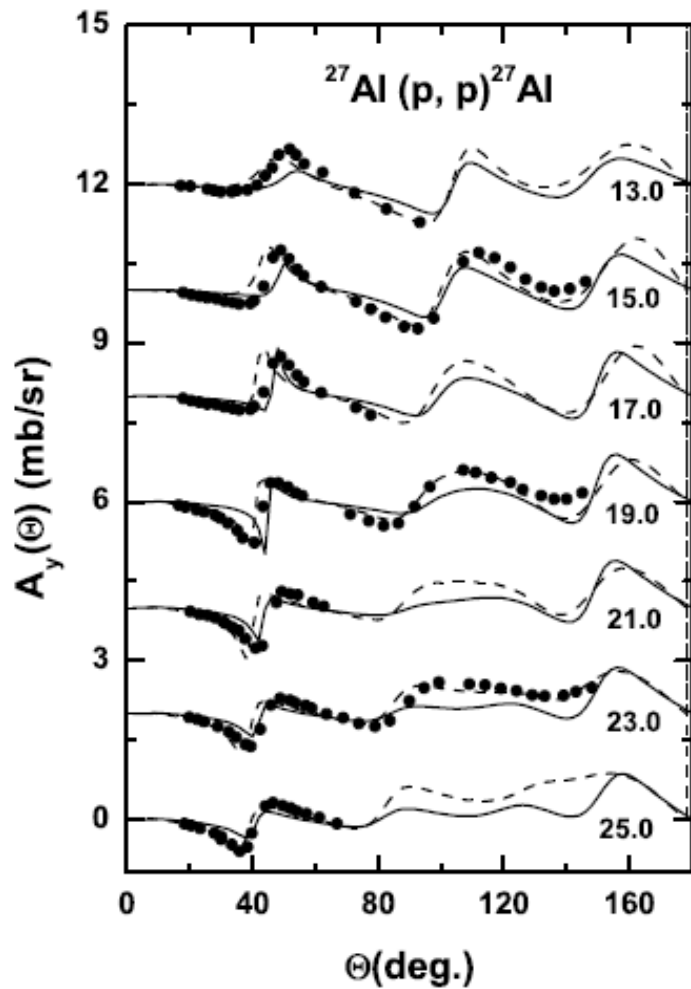
Target mass number (A): ^{12}C — ^{238}U 28 nuclei

Induced nuclei: n, p

Improved LDA









Summary

- The relativistic microscopic optical potential is obtained from DBHF G matrix in nuclear matter
- The OMP is of density, asymmetry parameter and energy dependence, LDA is used for finite nuclei. The RMOP could well describe the $p - A$ scattering data and isospin dependence of the RMOP.
- Microscopic optical potential for nucleus-nucleus elastic scattering, which includes the real and imaginary parts is obtained by folding with the density.
- New microscopic MOP from DBHF G matrix with density, energy and asymmetry dependence are available and under investigation



恭贺
卓益忠老师八十华诞！

福如东海
寿比南山



Thanks